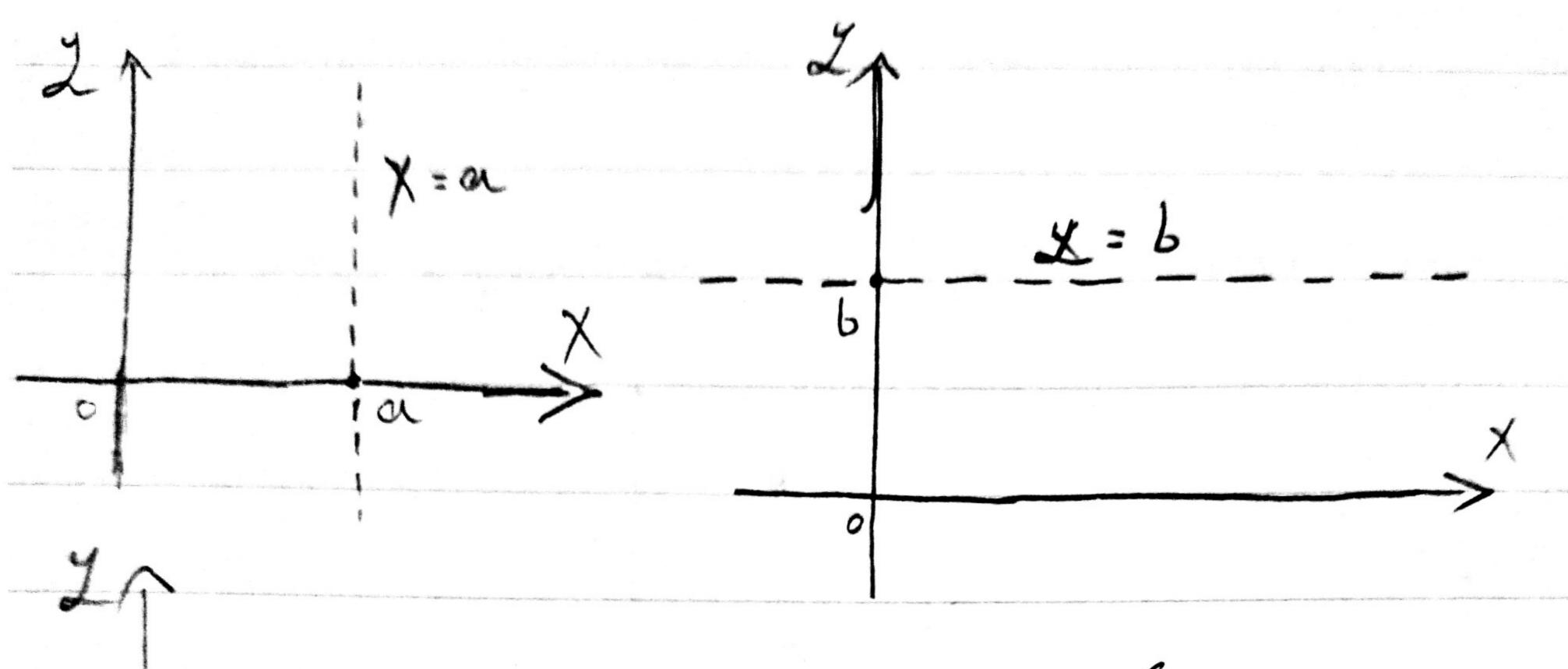
TWo fold (Double) equ of two stright Lines:



The two lines
$$L_1$$
: $\alpha_1 X + b_1 y + C_1 = 0$

$$\begin{cases} L_2 : \alpha_2 X + b_2 y + C_2 = 0 \end{cases}$$

arp

$$\frac{1}{t} \operatorname{an} \theta = \frac{m_2 - m_1}{1 + m_1 m_2}$$

Any Lines //
$$(1 + 0)$$
 is given by $4x - 5y + K = 0$
(1,2)

$$4 -) 0 + K = 0$$

The homogeneous eyn of 2nd degree in X, y represents two lines pussing thro. ax2+2hxy+by2=0 ->x X2 de émil

b(=) + 2h(=)+ a = 0

 $\mathcal{Z} = \left(\frac{-h + 1h^2 - \alpha b}{b}\right) \chi$

 $y=m_1 x$ $y=m_2 x$

Provided haub >0

ت تعمل خطف الزند المعبر بكونه أكبر من أكاسا وى صغر

$$EX$$
; Find the two lines represented by $\chi^2 - 7X\chi + 10 X' = 0$ $(y-2X)(y-5X) = 0$ $\chi = 2X$ & $\chi = 5X$

$$M_1 M_2 = \frac{\alpha}{6}$$

The angle of bet. the two lines *

$$t_{\alpha P} \theta = \frac{m_2 - m_1}{1 + m_1 m_2} = \frac{(m_2 - m_1)^2}{1 + m_1 m_2}$$

$$= \frac{\sqrt{(m_1 + m_1)^2 - 4m_1m_2}}{1 + m_1m_2}$$

$$tan\theta = \sqrt{\frac{4h^2}{b^2} - 4\frac{a}{b}} = \frac{2(h^2 - ab)}{1 + \frac{a}{b}}$$

$$tan\theta = 2\sqrt{\frac{49}{4}-10} = \frac{3}{11}$$

The double eyn of the bisectors tound of @ ()

$$\left(\frac{2-m_1 \times 1}{\sqrt{1+m_1^2}}\right) = \pm \frac{2-m_2 \times 1}{\sqrt{1+m_2^2}}$$

$$\frac{2 - m_1 \chi}{\sqrt{1 + m_1^2}} \frac{2 - m_2 \chi}{\sqrt{1 + m_1^2}} \left(\frac{2 - m_1 \chi}{\sqrt{1 + m_1^2}} + \frac{2 - m_2 \chi}{\sqrt{1 + m_1^2}} \right) = 0$$

$$\frac{(\chi - m_1 \chi)^2}{1 + m_1^2} = \frac{(\chi - m_2 \chi)^2}{1 + m_2^2} = 0$$

$$(1+m_1^2)(2^2+m_1^2)^2 - 2m_1(2) - (1+m_1^2)(2^2-2m_2)(2^2+m_1^2)^2 = 0$$

$$(m_1 + m_2)(\chi^2 - \chi^2) + 2(m_1 m_2 - 1)\chi \chi = 0$$

$$\frac{-2h}{b}(x^2-y^2) + 2(\frac{a}{b}-1)xy = 0$$
 (*1

$$\frac{3}{a} \frac{\chi^2 - \chi^2}{a - b} = \frac{\chi \chi}{h}$$

XI-Prove that the two lines thro, and make an angle with the line X-y=0 is given by $X^2 \pm 2Xy \operatorname{Sec2} x + y^2 = 0$

$$ax^2 + 2hxy + by^2 = 0$$

$$X - y = 0 \implies X + y = 0$$

 $X^2 - y^2 = 0 - - - (1)$

But the eyn of the bisectors
$$X^2-y^2 = \frac{\alpha-b}{h} \times y ----(2)$$

$$(1) = (2)$$

$$\frac{a-b}{b} = 0 \implies (a=b)$$

$$ton 2d = \frac{2\sqrt{h^2-\alpha^2}}{2\alpha}$$

$$a^2 + an^2 = h^2 - a^2$$
 $h^2 = a^2 (+ an^2 + 1)$

$$h = \pm \alpha Scc_2d$$

dx2 ±2 dsec2d. Xy +dy ===